

## COURSE SPECIFICATION FORM

<b>DEPARTMENT OF: Mathematics</b>				<b>Academic Session: 2017-18</b>	
<b>Course Code:</b>	MT1940	<b>Course Value:</b>	0.5	<b>Status:</b> (ie: Core, or Optional)	Mandatory for G100, G103, G1G3 and Mathematics majors
<b>Course Title:</b>	Numbers and Functions			<b>Availability:</b> (state which teaching terms)	Term 1
<b>Prerequisites:</b>	A-level Mathematics or equivalent			<b>Recommended:</b>	None
<b>Co-ordinator:</b>					
<b>Course Staff</b>					
<b>Aims:</b>	<ul style="list-style-type: none"> <li>• To kindle an interest in analysis, and to provide a taste of what the subject is about;</li> <li>• To give a user-friendly introduction to key ideas of analysis, illustrated with copious examples;</li> <li>• To provide a structure that enables students to gain confidence in handling concepts in analysis.</li> </ul>				
<b>Learning Outcomes:</b>	<p>On completion of the course, the student should be able to:</p> <ul style="list-style-type: none"> <li>• appreciate the significance of the completeness property distinguishing <b>R</b> from <b>Q</b>;</li> <li>• find sups and infs of elementary sets;</li> <li>• find out whether a given (simply defined) function is continuous at a point, and apply properties of continuous functions in examples;</li> <li>• determine whether a given (simple) sequence tends to a limit, using monotonicity when appropriate;</li> <li>• find limits of sequences defined recursively.</li> </ul>				
<b>Course Content:</b>	<p><b>The real number system:</b> The natural numbers <b>N</b>, the binomial theorem using induction. The integers <b>Z</b> and the rational field <b>Q</b>. Order properties, manipulation of inequalities, the triangular inequality. Irrationality of <math>\sqrt{2}</math>. Decimal representation of real numbers. Null sequences. Subsets, maximum, upper bound, least upper bound. Every non-empty subset of the reals which is bounded above has a least upper bound. Bernoulli's inequality with applications.</p> <p><b>Continuity:</b> Discussion of continuity, continuity of <math>f</math> at a point. A continuous function is specified by its values at rational points. Discussion of <math>f(x) = 2^x</math>. Continuity on an interval. A continuous function on a closed interval. Discussion of the intermediate value theorem.</p> <p><b>Sequences:</b> Limits of sequences, limits of sequences defined recursively. Monotonic sequence theorem. Connection with continuity.</p>				
<b>Teaching &amp; Learning Methods:</b>	33 hours of lectures and examples classes, 6 hours tutorials. 111 hours of private study, including work on problem sheets and examination preparation. This may include discussions with the course leader if the student wishes.				
<b>Key Bibliography:</b>	Numbers and Functions (steps into analysis) – R P Burn (Cambridge 2000). <i>Library Ref. 515.23 BUR</i> Yet Another Introduction to Analysis – Victor Bryant (Cambridge 1990). <i>Library Ref. 515 BRY</i>				
<b>Formative Assessment &amp; Feedback:</b>	Formative assignments in the form of 11 problem sheets. The students will receive feedback as written comments on their attempts.				
<b>Summative Assessment:</b>	<p><b>Exam (%)</b> A two-hour paper: 80%</p> <p><b>Coursework (20%)</b> Attempting problem sheets: 10%; a 45 minute test in January: 10%</p>				

Updated September 2017

The information contained in this course outline is correct at the time of publication, but may be subject to change as part of the Department's policy of continuous improvement and development. Every effort will be made to notify you of any such changes.